Semantic Change and Extension Enforcement in Abstract Argumentation

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Background

Dung's Framework Extension Enforcement

Using Semantic Change for Extension Enforcement Motivational Example Generalizing Enforcement Operators Empirical Evaluation

Conclusion





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Dung's Framework [Dung 1995]

- **AF** are digraphs F = (A, R), with A the arguments and $R \subseteq A \times A$ the attacks
- Extension-based semantics : determining sets of jointly acceptable arguments





Dung's Framework [Dung 1995]

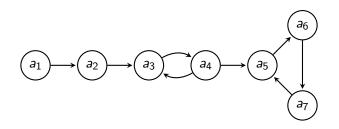
- **AF** are digraphs F = (A, R), with A the arguments and $R \subseteq A \times A$ the attacks
- Extension-based semantics : determining sets of jointly acceptable arguments

Many semantics. A set $E \subseteq A$ is

- **cf** w.r.t. F if $\nexists a_i, a_j \in S$ s.t. $(a_i, a_j) \in R$;
- ▶ ad w.r.t. *F* if *S* is cf and *S* defends each $a_i \in S$;
- ▶ **na** w.r.t. *F* if *S* is a maximal cf set (w.r.t. \subseteq);
- **co** w.r.t. *F* if *S* is ad and *S* contains all the arguments that it defends;
- ▶ **pr** w.r.t. *F* if *S* is a maximal co extension (w.r.t. \subseteq);
- st w.r.t. F if S is cf and $S_R^+ = A$;
- gr w.r.t. F if S is a minimal co extension (w.r.t. \subseteq);

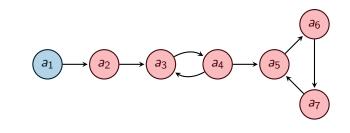








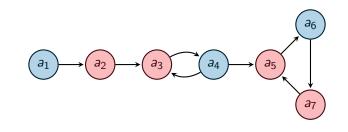




 $\mathit{Ext}_{\mathit{gr}}(F) = \{\{a_1\}\}$



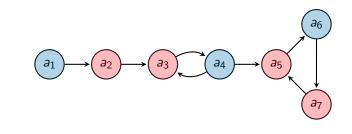




 $Ext_{st}(F) = \{\{a_1, a_4, a_6\}\}$



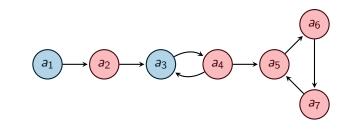




$$Ext_{pr}(F) = \{\{a_1, a_4, a_6\}, \{a_1, a_3\}\}$$



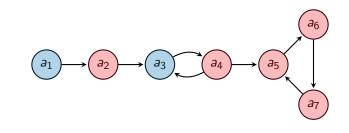




$Ext_{pr}(F) = \{\{a_1, a_4, a_6\}, \{a_1, a_3\}\}$







$Ext_{co}(F) = \{\{a_1, a_4, a_6\}, \{a_1, a_3\}, \{a_1\}\}$





Distance between Semantics [Doutre and Mailly 2016]

$$Inc(\Sigma)$$
 with $\Sigma = \{cf, ad, na, st, pr, co, gr\}.$

$$\begin{array}{ccc} pr \rightarrow co \rightarrow ad \rightarrow cf \\ \uparrow & \uparrow & \uparrow \\ st & gr & na \end{array}$$

Σ -Inclusion Difference Measure

 $\delta_{Inc,\Sigma}(\sigma_i,\sigma_j)$ is the length of the shortest non-oriented path between σ_i and σ_j in $Inc(\Sigma)$

• e.g.
$$\delta_{Inc,\Sigma}(st, ad) = 3$$
, $\delta_{Inc,\Sigma}(pr, gr) = 2$, and $\delta_{Inc,\Sigma}(co, pr) = 1$





Strict (resp. Non-Strinct) Enforcement

$$\left. \begin{array}{c} F = \langle A, R \rangle \\ E \subseteq A \end{array} \right\} \quad \Longrightarrow \quad F' = \langle A', R' \rangle$$

such that E is an extension (resp. included in an extension) of F'





Expansions of AFs [Baumann and Brewka 2010]

Given
$$F = \langle A, R \rangle, F' = \langle A', R' \rangle$$
,

- F' is a **normal expansion** of F iff $A \subset A'$ and $R' \cap (A \times A) = R$
- F' is a weak expansion of F iff F' is a normal expansion of F s.t. ∀(a_i, a_j) ∈ R'\R, a_j ∉ A
- F' is a **strong expansion** of F iff F' is a normal expansion of F s.t. $\forall (a_i, a_j) \in R' \setminus R$, $a_i \in A' \setminus A$





Enforcement Based on Expansions [Baumann and Brewka 2010]

Strict (resp. Non-Strinct) Normal (resp. Weak, Strong) Enforcement

$$\left. \begin{array}{c} F = \langle A, R \rangle \\ E \subseteq A \end{array} \right\} \implies F' = \langle A', R' \rangle$$

such that E is an extension (resp. included in an extension) of F' and F' is a normal (resp. weak, strong) expansion of F





• Using $\sigma = st$, how to enforce $E = \{a_2, a_3\}$ in F?

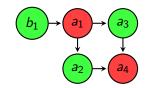






• Using $\sigma = st$, how to enforce $E = \{a_2, a_3\}$ in F?









Argument-Fixed and General Enforcement [Coste-Marquis et al 2015]

- Argument-fixed enforcement : perform a strict or non-strict enforcement without modifying the set of arguments (modifying attacks is possible)
- General enforcement : perform a strict or non-strict enforcement by any possible means (adding arguments, modifying attacks)





Example of Argument-Fixed (General) Enforcement

• Using $\sigma = st$, how to enforce $E = \{a_2, a_3\}$ in F?







Example of Argument-Fixed (General) Enforcement

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Minimal Change Extension Enforcement [Baumann 2012]

Minimal enforcement : F' must be as close as possible from F, closeness is measured with Hamming distance

$$d_{H}(F,F') = |(R \setminus R') \cup (R' \setminus R)|$$

• Characteristics : given an enforcement operator Op, a semantics σ , and AF $F = \langle A, R \rangle$ and $E \subseteq A$, $\mathbf{V}_{\sigma, \mathbf{Op}}^{\mathsf{F}}(\mathsf{E})$ is the function which computes the minimal change to enforcement E in F w.r.t. σ





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Fixed Semantics Enforcement vs Semantic Change

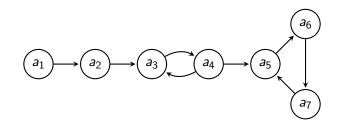
- Existing enforcement methods consider that
 - either the semantics doesn't change
 - or the new semantics is given as a parameter of the operator no justification of *why* it changes nor *how* the new one is chosen

Idea of Semantic Change for Enforcement

- Define enforcement operators equipped with a set of possible semantics
- Choose the best new semantics in this set to obtain minimal change enforcement







- Current semantics : $\sigma = st$, $Ext_{st}(F) = \{\{a_1, a_4, a_6\}\}$
- Goal : enforcing $E = \{a_1, a_3\}$
- Without semantic change : the graph has to be modified
- With semantic change : switch semantics from st to pr, since E ∈ Ext_{pr}(F) = {{a₁, a₃}, {a₁, a₄, a₆}}. No change of the graph at all





Enforcement With Semantic Change

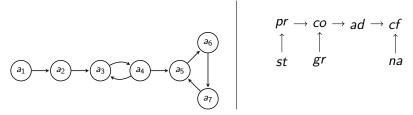
$$\left. \begin{array}{c} F = \langle A, R \rangle \\ \sigma \\ \Sigma = \{ \sigma'_1, \dots, \sigma'_k \} \\ E \subseteq A \end{array} \right\} \implies \left\{ \begin{array}{c} F' = \langle A', R' \rangle \\ \sigma' \in \Sigma \end{array} \right.$$

such that

- *E* is a σ' -extension (resp. included in an extension) of *F'*
- F' is as close as possible from F
- \blacktriangleright σ' is as close as possible from σ







•
$$\sigma = st$$
, $Ext_{st}(F) = \{\{a_1, a_4, a_6\}\}, E = \{a_1, a_3\}$

•
$$F = F'$$
, so $d_H(F, F') = 0$ is minimal

•
$$\delta_{Inc,\Sigma}(st, pr) = 1 < \delta_{Inc,\Sigma}(st, co) = 2 < \delta_{Inc,\Sigma}(st, ad) = 3 < \delta_{Inc,\Sigma}(st, cf) = 4$$





Question : When is it useful/successful to use semantic change?

- Useful when it guarantees that enforcement with σ_j can be realized with strictly less changes of the graph than with σ_i
 - A threshold can be considered : useful when the change with σ_i is at least $\tau\%$ "easier" than with σ_i





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- Guarantee : our method can't give a worse result than "classical" enforcement
- How to determine when it gives a better result?





General Idea

- For a large set of F and E, enforce E in F for $\sigma \in \Sigma$
- For each instance, compute $V_{\sigma,Op}^{\mathcal{F}}(E)$ for all $\sigma \in \Sigma$
- For each pair of semantics (σ_i, σ_j) , it is useful to change the semantics when $V^F_{\sigma_i, Op}(E) \leq 0.9 \times V^F_{\sigma_i, Op}(E)$

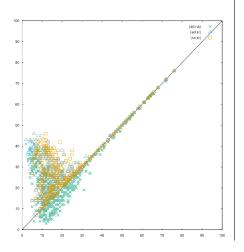
Details

- The instances come from [Wallner et al, AAAI 2016] : 400 instances for each |A| ∈ {50, 100, 150, 200, 250, 300}
- Enforcement operator : strict argument-fixed operator, {ad, st, co} come from [Wallner et al], home-made implementation for na





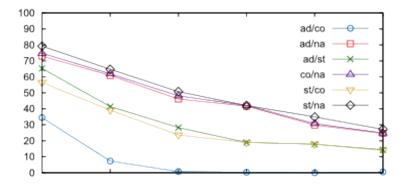
Representative Sample of the Results



- ▶ |*A*| = 50
- Similar results for (st, na) and (na, co), only (ad, co) gives a lot of instances close to the diagonal
- ▶ Similar results for other |A|







Percentage of success depending on |A|





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- Generalizing enforcement operators to benefit from semantic change
 - Experimental evaluation shows that semantic change brings better results in a lot of situations
- Not in the talk : we have extended Baumann's study of characteristics





About characteristics

 Some characteristics are still unknown for several semantics and enforcement operators

About the experimental evaluation

- Conduct similar studies with other semantics and operators
- Success rate with other values than 0.9

About implementations

 Generalize the software systems : compute the characteristics for different semantics and operators before performing enforcement, to be able to choose the best one (w.r.t. change of the graph)





Future work (2/2)

Deeper questions on extension enforcement

- ► The success rate seems to decrease when |A| increases. Does it decrease to 0 or is there a minimal?
- Our evaluation of success is only experimental. Are there properties related to success?
 - Some graphs structures, pattern, etc which would guarantee that semantic change is/isn't successful

Semantic change for other operations

- Revision of AFs [Coste-Marquis et al, KR'14] returns a set of AFs, with two notions of minimality (difference of the graph and cardinality of the result)
- Can we use semantic change to improve the minimality w.r.t. one (or both) of these notions?



